Pairing and Phase Separation in a Polarized Fermi Gas

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We report the observation of pairing in a gas of atomic fermions with unequal numbers of two components. Beyond a critical polarization, the gas separates into a phase that is consistent with a superfluid paired core surrounded by a shell of normal unpaired fermions. The critical polarization diminishes with decreasing attractive interaction. For near-zero polarization, we measured the parameter \( \beta = -0.54 \pm 0.05 \), describing the universal energy of a strongly interacting paired Fermi gas, and found good agreement with recent theory. These results are relevant to predictions of exotic phases of quark matter and of strongly magnetized superconductors.

Fermion pairing is the essential ingredient in the Bardeen, Cooper, and Schrieffer (BCS) theory of superconductivity. In conventional superconductors, the chemical potentials of the two spin states are equal. There has been great interest, however, in the consequences of mismatched chemical potentials that may arise in several important situations, including, for example, magnetized superconductors (1–3) and cold dense quark matter at the core of neutron stars (4). A chemical potential imbalance may be produced by several mechanisms, including magnetization in the case of superconductors, mass asymmetry, or unequal numbers. Pairing is qualitatively altered by the Fermi energy mismatch, and there has been considerable speculation regarding the nature and relative stability of various proposed exotic phases. In the Fulde-Ferrel-Larkin-Ovchinnikov (FFLO) phase (2, 3), pairs possess a nonzero center-of-mass momentum that breaks translational invariance, whereas the Sarma (1), or the breached pair (5), phase is speculated to have gapless excitations. A mixed phase has also been proposed (6–8) in which regions of a paired BCS superfluid are surrounded by an unpaired normal phase. Little is known experimentally, however, because of the difficulty in creating magnetized superconductors. Initial evidence for an FFLO phase in a heavy-fermion superconductor has only recently been reported (9, 10).

Oppurtunities for experimental investigation of exotic pairing states have expanded dramatically with the recent realization of the Bose-Einstein condensate (BEC)–BCS crossover in a two spin state mixture of ultracold atomic gases. Recent experiments have demonstrated both superfluidity (11–13) and pairing (14–17) in atomic Fermi gases. We report the observation of pairing in a polarized gas of \(^6\)Li atoms. Above an interaction-dependent critical polarization, we observed a phase separation that is consistent with a uniformly paired superfluid core surrounded by an unpaired shell of the excess spin state. Below the critical polarization, the spatial size of the gas was in agreement with expectations for a universal, strongly interacting paired Fermi gas.

Our methods for producing a degenerate gas of fermionic \(^6\)Li atoms (18, 19) and the realization of the BEC-BCS crossover at a Feshbach resonance (17) have been described previously (20). An incoherent spin mixture of the \( F = \frac{3}{2}, m_F = \frac{3}{2} \) (state \( |1\rangle \)) and the \( F = \frac{1}{2}, m_F = \frac{1}{2} \) (state \( |2\rangle \)) sublevels (where \( F \) is the total spin quantum number and \( m_F \) is its projection) is created by radio frequency (rf) sweeps, where the relative number of the two states can be controlled by the rf power (20). The spin mixture is created at a magnetic field of 754 G, which is within the broad Feshbach resonance located near 834 G (21, 22). The spin mixture is evaporatively cooled by reducing the depth of the optical trap that confines it, and the magnetic field is ramped adiabatically to a desired field within the crossover region. States \( |1\rangle \) and \( |2\rangle \) are sequentially and independently imaged in the trap by absorption (20). Analysis of these images provides measurement of \( N_i \) and polarization \( P = (N_1 - N_2)/(N_1 + N_2) \), where \( N_i \) is the number of atoms in state \( |i\rangle \). We express the Fermi temperature, \( T_F \), in terms of the majority spin state, state \( |1\rangle \), as \( k_B T_F = \hbar \omega_c (6N_i)^{1/3} \), where \( \hbar = 2\pi \langle u_1^2 u_2 \rangle^{3/2} \) is the mean harmonic frequency of the cylindrically symmetric confining potential with radial and axial frequencies \( \omega_c \) and \( \omega_0 \), respectively. For \( P = 0 \), we find that \( N_1 \approx N_2 \approx 10^8 \), giving \( T_F \approx 400 \) nK for our trap frequencies. Because of decreasing evaporation efficiency with increasing polarization, there is a correlation between \( P \) and total atom number (fig. S1).

For fields on the low-field (BEC) side of resonance, real two-body bound states exist, and molecules are readily formed by three-body recombination. For the case of \( P = 0 \), a molecular Bose-Einstein condensate (MBEC) is observed to form with no detectable thermal molecules (17). On the basis of an estimated MBEC condensate fraction of \( >90\% \), we place an upper limit on the temperature \( T < 0.1 T_F \) at a field of 754 G (17). However, the gas is expected to be cooled further during the diabatic ramp for final fields greater than 754 G (17). By using similar experimental methods, we previously measured the order parameter of the gas in the BCS regime and found good agreement with \( T = 0 \) BCS theory (17), indicating that the gas was well below the critical temperature for pairing.

Images of states \( |1\rangle \) and \( |2\rangle \) at a field of 830 G are shown (Fig. 1) for relative numbers...
corresponding to \( P = 0.14 \). The strength of the two-body interactions is characterized by the dimensionless parameter \( k_p a \), where \( k_p \) is the Fermi wave vector and \( a \) is the s-wave scattering length. For a field of 830 G, \( k_p a \) is greater than 10, corresponding to a unitarity limited interaction. We contend that the gas has separated into a uniformly paired, unpolarized inner core surrounded by a shell of the excess, unpaired state \(|1\rangle\) atoms. In this case, the distribution of the difference, \(|1\rangle – |2\rangle\) (Fig. 1), represents the location of these unpaired state \(|1\rangle\) atoms.

Axial profiles of a sequence of images (Fig. 2) correspond to increasing values of \( P \), again for 830 G. These axial profiles are the result of integrating the column density over the remaining radial coordinate. They are insensitive to the effect of finite imaging resolution in the radial dimension as well as to probe-induced radial heating of the second image in the sequence (20). On the left of Fig. 2 are distributions for both states \(|1\rangle\) and \(|2\rangle\), whereas the right side shows the corresponding difference distributions. Also shown in Fig. 2 are fits to a noninteracting \( T = 0 \) integrated Thomas-Fermi (T-F) distribution for fermions, 

\[ A \left(1 - \frac{z}{R_z}\right)^2, \]

where \( A \) and \( R \) are adjustable fitting parameters and \( z \) is the axial position. Although the distributions are expected to differ somewhat from that of a noninteracting Fermi gas, we find that the fits are qualitatively good and provide a useful measure of the spatial size of the distributions. For \( P = 0 \) (Fig. 2A), the two spin components have identical distributions. We previously found that the gas was paired under the same conditions (17). As \( P \) increases (Fig. 2B), the peak height and width of the state \(|2\rangle\) distributions initially diminish with respect to state \(|1\rangle\), but their shapes are not fundamentally altered. When the polarization is increased beyond a critical value, however, the shapes of the two clouds become qualitatively different (Fig. 2C): The inner core, reflected by the distribution of the \(|2\rangle\) atoms, is squeezed and becomes taller and narrower. This narrowing is noticeable in the wings of the state \(|2\rangle\) distribution in comparison with the T-F fit. The squeezing of the state \(|2\rangle\) distribution is accompanied by the excess, unpaired state \(|1\rangle\) atoms being expelled from the center of the trap. These unpaired atoms form a shell that surrounds the inner core. As \( P \) approaches 1 (Fig. 2D), the contrast in the center hole in the difference distribution decreases because of the contribution to the axial density of unpaired atoms in the shell surrounding the core. The observation of difference distributions with a center hole and two peaks on either side is consistent with phase separation. Although more exotic redistributions of atoms cannot be ruled out, a separation between a uniformly paired phase and the excess unpaired atoms is the simplest explanation and is consistent with theoretical predictions (6–8).

To gain a more quantitative understanding of the phase separation as a function of \( P \), we plot the ratio \( R/R_{TF} \) against \( P \), where \( R_{TF} = \left( \frac{\hbar^2 T}{m \omega_a} \right)^{1/2} \) is the axial T-F radius for noninteracting fermions (23) and \( m \) is the atomic mass. \( \omega_a = 2\pi v_a \) and \( T_a \) is calculated for each state from the measured numbers \( N_1 \) and \( N_2 \). Figure 3 shows the results for all of the 830 G data. At a critical polarization \( P_c = 0.09 \pm 0.025 \), \( R/R_{TF} \) for states \(|1\rangle\) and \(|2\rangle\) diverges in opposite directions from its value at small \( P \), \( R/R_{TF} \) for state \(|2\rangle\), which corresponds to the distribution of the pairs, decreases continuously to \( \sim 0.4 \) for the maximum attained polarization of \( P \sim 0.86 \). For state \(|1\rangle\), \( R/R_{TF} \) jumps from its initial value to near unity at the critical polarization. Because \( P = 1 \) corresponds to a noninteracting gas, one expects \( R/R_{TF} \) to approach unity in this limit.

In the case of \( P \approx 0 \), the observation that the axial extent of the paired cloud is smaller than that of a noninteracting Fermi gas can be explained by the universal energy of strongly interacting paired fermions at the unitarity limit, where \( k_p a \gg 1 \) (24). In this limit, the chemical potential of the gas is believed to have the universal form \( E_0(1 + \beta)^3 \), where \( \beta \) is a universal many-body parameter that increases continuously to \( \sim 0.4 \) for the maximum attained polarization of \( P \sim 0.86 \). For state \(|1\rangle\), \( R/R_{TF} \) jumps from its initial value to near unity at the critical polarization. Because \( P = 1 \) corresponds to a noninteracting gas, one expects \( R/R_{TF} \) to approach unity in this limit.

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can be determined from $\beta = (R/R_{TF})^2 - 1$ (25–27). For $P$ near zero, we found that $R/R_{TF} = 0.825 \pm 0.02$, giving $\beta = -0.54 \pm 0.05$ (uncertainties discussed in Fig. 3 legend). This value is in excellent agreement with previous measurements (24, 26, 28, 29) but with substantially improved uncertainty. Our measurement is also consistent with $\beta = -0.58 \pm 0.01$ obtained from two Monte Carlo calculations (8, 30, 31) and with $\beta = -0.545$ from a calculation reported in (27). Not surprisingly, the measurement is in disagreement with $\beta = -0.41$ obtained with BCS mean-field theory (27).

We believe that the data are consistent with a quantum phase transition from a homogenous paired superfluid state to a superfluid-normal phase separated state. For $P = 0$, the excellent agreement between the measured value of $\beta$ and theory, combined with our previous measurement of pair correlations in an unpolarized gas (17), is strong evidence that the gas is paired. Furthermore, superfluidity has been observed in the same system under similar conditions (11–13). The fact that the size of the gas, which is strongly dependent on the gas being paired, does not change appreciably for $0 < P < P_c$ suggests that it may remain paired in this regime, which is remarkable (32). For $P > P_c$, the excess unpaired atoms prefer to reside in a shell outside the inner core. Such a phase separation may be explained in the BEC regime (33) where the atoms and weakly bound dimers are believed to have a large repulsive three-body interaction (34); however, application of this theory to the strongly interacting regime would be incorrect because it also gives a large repulsive dimer-dimer interaction (34) that is inconsistent with a negative value of $\beta$. Therefore, we conclude that the phase separation is a consequence of the energy cost of accommodating unpaired atoms within the paired core (6–8). Vortices have also been used to explore superfluidity in $^6$Li with mismatched Fermi surfaces (35). Although hints of phase separation are reported in that work, a critical polarization was not observed.

We also performed the experiment at 920 G, which is on the BCS side of the resonance where $k_F a = -1.1$. We found a phase separation at this field as well. However, the value of $R/R_{TF}$ at $P = 0$ is larger, $0.92 \pm 0.02$, a consequence of smaller but still strong interactions, and the critical polarization for phase separation is considerably smaller, $P_c < 0.03$, consistent with zero to within our experimental sensitivity. Observation of phase separation at small $P$ demonstrates the sensitivity of our determination of phase separation. In the BEC regime at a field of 754 G where $k_F a = 0.6$, we find that $P_c$ is somewhat larger than 0.10, but at this field probe-induced radial heating prevents an accurate determination (20). The critical polarization value diminishes going from the BEC to BCS regimes, as expected (8). In the BCS regime, very little Fermi energy mismatch is tolerated before phase separation occurs. For samples prepared at higher temperature ($T \approx 0.7T_F$), no phase separation was observed.

The nature of the coexistence phase where $P < P_c$ is still unknown, so the existence of the FFLO and the breached pair states are not excluded by these observations. Recent calculations suggest that a homogeneous gapless superfluid state may be preferred for small polarizations in the unitarity regime (8). These results help to clarify the long-open question of how Fermi superfluids respond to mismatched Fermi surfaces.

References and Notes

6. Materials and methods are available as supporting material on Science Online.
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20. Materials and methods are available as supporting material on Science Online.
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